

Pre – Calculus 30
Introduction to Transformations

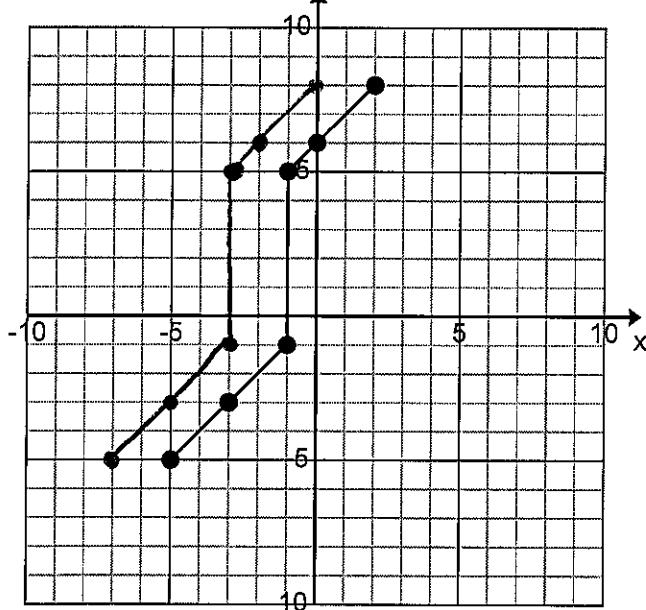
Name: Key.

For each graph apply the following transformation and graph the function on the same grid.

1. Translate the graph 2 units to the left

Original Point	Image Point
(-5, -5)	(-7, -5)
(-3, -3)	(-5, -3)
(-1, -1)	(-3, -1)
(-1, 5)	(-3, 5)
(0, 6)	(-2, 6)
(2, 8)	(0, 8)

"Horizontal translation."



For the new graph state the

Domain: $\{x | -7 \leq x \leq 0, x \in \mathbb{R}\}$ $[-7, 0]$

Range: $\{y | -5 \leq y \leq 8, y \in \mathbb{R}\}$ $[-5, 8]$

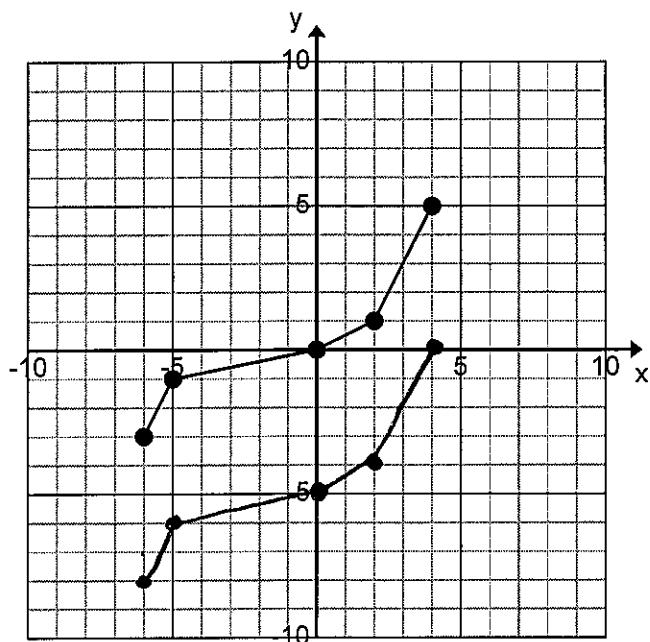
X-intercept $(-3, 0)$

Y-intercept $(0, 8)$

2. Translate the graph 5 units down

Original Point	Image Point
(-6, -3)	(-6, -8)
(-5, -1)	(-5, -6)
(0, 0)	(0, -5)
(2, 1)	(2, -4)
(4, 5)	(4, 0)

"Vertical translation."



For the new graph state the
Domain: $\{x \mid -6 \leq x \leq 4, x \in \mathbb{R}\}$ $[-6, 4]$

Range: $\{y \mid -8 \leq y \leq 0, y \in \mathbb{R}\}$ $[-8, 0]$

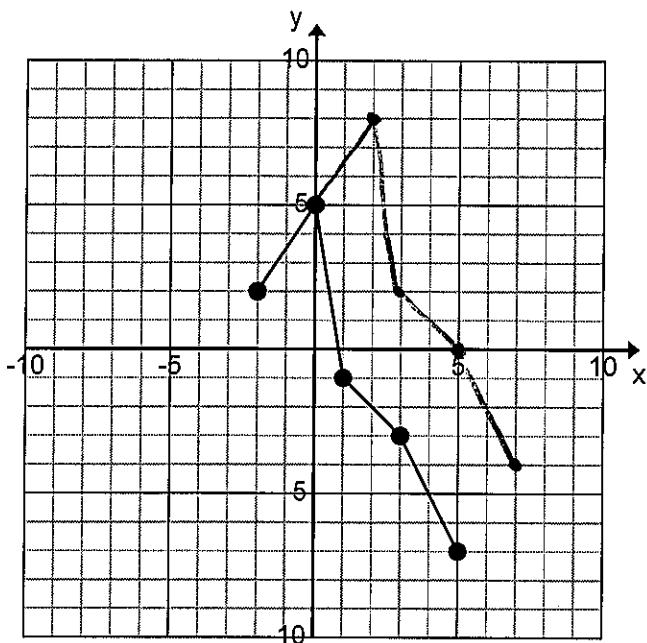
X-intercept: $(4, 0)$

Y-intercept: $(0, -5)$

3. Translate the graph 2 units right and 3 units up

Original Point	Image Point
(-2, 2)	(0, 5)
(0, 5)	(2, 8)
(1, -1)	(3, 2)
(3, -3)	(5, 0)
(5, -7)	(7, -4)

"Vertical and horizontal translations."



For the new graph state the

Domain: $\{x | 0 \leq x \leq 7, x \in \mathbb{R}\}$ $[0, 7]$

Range: $\{y | -4 \leq y \leq 8, y \in \mathbb{R}\}$ $[-4, 8]$

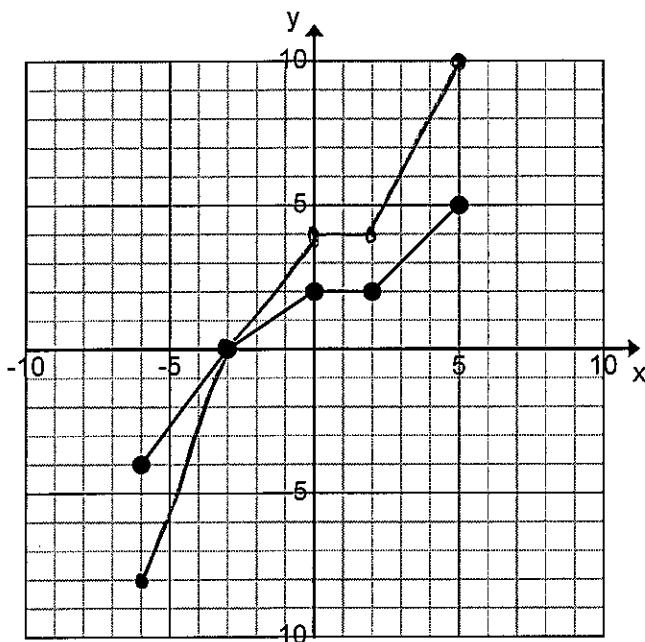
X-intercept: $(5, 0)$

Y-intercept: $(0, 5)$

4. Leaving the x-value the same, multiply the y-value of each point by 2.

Original Point	Image Point
(5, 5)	(5, 10)
(2, 2)	(2, 4)
(0, 2)	(0, 4)
(-3, 0)	(-3, 0)
(-6, -4)	(-6, -8)

"Vertical stretch
by a factor of 2."



For the new graph state the

Domain: $\{x \mid -6 \leq x \leq 5, x \in \mathbb{R}\}$ $[-6, 5]$

Range: $\{y \mid -8 \leq y \leq 10, y \in \mathbb{R}\}$ $[-8, 10]$

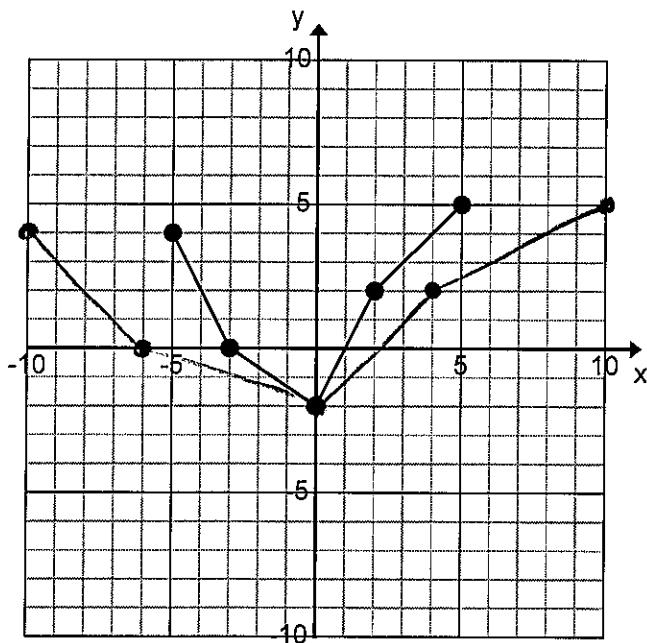
X-intercept: $(-3, 0)$

Y-intercept: $(0, 4)$

5. Leaving the y-value the same, multiply the x-value of each point by 2.

Original Point	Image Point
(-5, 4)	(-10, 4)
(-3, 0)	(-6, 0)
(0, -2)	(0, -2)
(2, 2)	(4, 2)
(5, 5)	(10, 5)

"Horizontal stretch by a factor of 2."



For the new graph state the

Domain: $\{x \mid -10 \leq x \leq 10, x \in \mathbb{R}\}$ $[-10, 10]$

Range: $\{y \mid -2 \leq y \leq 5, y \in \mathbb{R}\}$ $[-2, 5]$

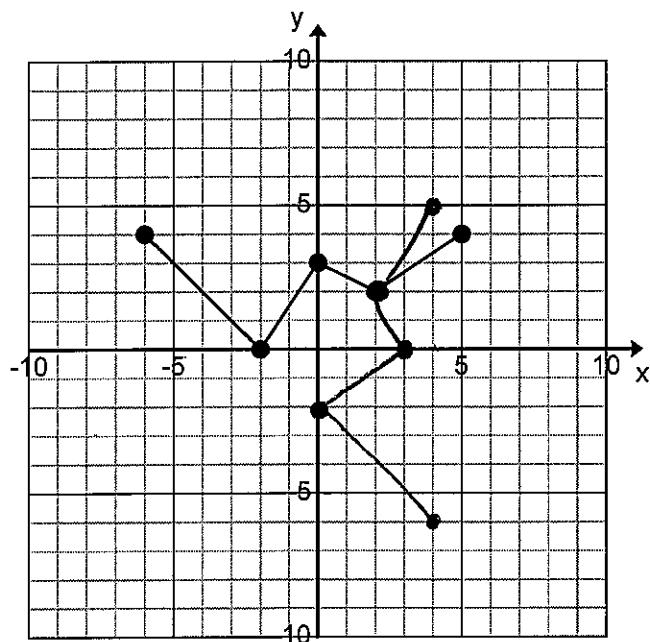
X-intercept: $(-6, 0)$

Y-intercept: $(0, -2)$

6. Switch the x and y values for each point. Example (2, -3) becomes (-3, 2)

Original Point	Image Point
(-6, 4)	(4, -6)
(-2, 0)	(0, -2)
(0, 3)	(3, 0)
(2, 2)	(2, 2)
(5, 4)	(4, 5)

"Inverse"



For the new graph state the

Domain: $\{x | 0 \leq x \leq 4, x \in \mathbb{R}\}$ $[0, 4]$

Range: $\{y | -6 \leq y \leq 5, y \in \mathbb{R}\}$ $[-6, 5]$

X-intercept: $(3, 0)$

Y-intercept: $(0, -2)$