



2.3 The Quadratic Formula

There is a way to calculate the **roots** (zeros or x-intercepts) of any quadratic. It is called the Quadratic Formula or Equation.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



Ex.) Solve $x^2 + 2x - 3 = 0$ using the Quadratic Equation.

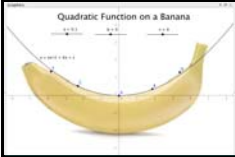


Steps: *Start by identifying the terms a, b and c
*Then, substitute the values into the Quadratic Equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(1)(-3)}}{2(1)}$$

$$x = \frac{-2 \pm \sqrt{16}}{2} = \frac{-2 \pm 4}{2} \begin{cases} x = \frac{-2+4}{2} = \boxed{1} (1,0) \\ x = \frac{-2-4}{2} = \boxed{-3} (-3,0) \end{cases}$$

Ex.) a) $x^2 + 4x - 1 = 0$

$a=1$
 $b=4$
 $c=-1$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-4 \pm \sqrt{(4)^2 - 4(1)(-1)}}{2(1)}$$

$$x = \frac{-4 \pm \sqrt{20}}{2}$$

$$x = \frac{-4 \pm 2\sqrt{5}}{2}$$

$$x = -2 \pm \sqrt{5} \text{ Exact Value}$$

$$x = 0.24$$

$$x = -4.24 \text{ Nearest Hundredth}$$

b) $x^2 - x + 4 = 0$

$a=1$
 $b=-1$
 $c=4$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

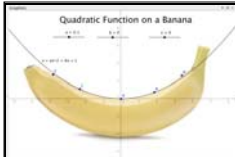


$$x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(1)(4)}}{2(1)}$$

$$x = \frac{1 \pm \sqrt{-15}}{2}$$

not possible

$\therefore \text{no } x\text{-intercepts}$

therefore

Ex.) Solve the following with the quadratic formula.

a) $x^2 + 4x - 2 = 0$

$a=1$
 $b=4$
 $c=-2$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-4 \pm \sqrt{(4)^2 - 4(1)(-2)}}{2(1)}$$

$$x = \frac{-4 \pm \sqrt{24}}{2}$$

$$x = \frac{-4 \pm 2\sqrt{6}}{2}$$

$$x = -2 \pm \sqrt{6} \text{ Exact}$$

$$x = 0.45$$

$$x = -4.45 \text{ Nearest Hundredth}$$

b) $x^2 - 5x + 4 = 0$


$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(4)}}{2(1)}$$

$$x = \frac{5 \pm \sqrt{9}}{2}$$

$$x = \frac{5 \pm 3}{2}$$


$$\frac{5+3}{2} = \frac{8}{2} = 4$$

$$\frac{5-3}{2} = \frac{2}{2} = 1$$



Quadratic Function on a Banana

Solving Quadratics NOT in the form $ax^2 + bx + c = 0$



Solving Quadratics NOT in the form $ax^2 + bx + c = 0$

If the Quadratic Equation is not in the form $ax^2 + bx + c = 0$, then it **must be converted** to this form first before solving! One side must equal zero.

Ex.) Solve each equation:

a) ~~$2x = 3(x-1)(x+1)$~~

$2x = 3(x^2 - 1)$

$2x = 3x^2 - 3$

$0 = 3x^2 - 2x - 3$

$a = 3$
 $b = -2$
 $c = -3$

$x = \frac{-(-2) \pm \sqrt{(-2)^2 - 4(3)(-3)}}{2(3)}$

$x = \frac{2 \pm \sqrt{40}}{6}$

$x = \frac{1 \pm \sqrt{10}}{3}$

$x = \frac{1 + \sqrt{10}}{3} = 1.39$
 $x = \frac{1 - \sqrt{10}}{3} = -0.72$

b) ~~$\frac{2}{3}x^2 + 1 = \frac{5}{6}x$~~

~~$-\frac{5}{6}x - \frac{5}{6}x$~~

$\frac{2}{3}x^2 - \frac{5}{6}x + 1 = 0$

$x = \frac{-(-5/6) \pm \sqrt{(-5/6)^2 - 4(2/3)(1)}}{2(2/3)}$

$x = \frac{5/6 \pm \sqrt{-71/36}}{4/3}$

no solutions
no x-int
no roots
no zeros

Pg. 254 # 3, 4, 5, 6, 7.