

Unit 5: Absolute Values, Reciprocals, Systems, Inequalities

5.6 Graphing Linear Inequalities in Two Variables

Equations
 =
 definite solutions (ie. $x = 2$)
 eg. $y = 8x - 3$

Inequalities
 $<, \leq, \geq, >$
 infinite solutions (represented by a **solution region**)
 eg. $y > 2x - 9$

$y = mx + b$

divide/multiply by a NEGATIVE, switch the inequality

Ex.) Graph $4x + 2y \geq 10$. Is $(1, 3)$ part of the solution?

$-4x \quad -4x$

$\frac{2y}{2} \geq \frac{-4x + 10}{2} \frac{10}{2}$

$y \geq -2x + 5$


"shade \geq the line"

$4x + 2y \geq 10$
 $4(3) + 2(4) \geq 10$
 $20 \geq 10$

$4(-1) + 2(-1) \geq 10$
 $-6 \not\geq 10$

$\geq \leq$ - solid line
 $> <$ - dotted line

Yes



Ex.) Graph $5x - 20y < 0$. Verify the solution region? $<$ - dotted line

$-5x$ $-5x$

$\frac{-20y}{-20} < \frac{-5x}{-20}$

* division by neg. switch inequality*

$y > \frac{1}{4}x$

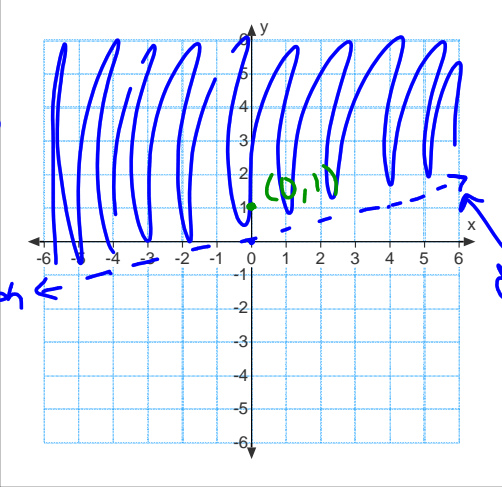
Shade $>$ graph \leftarrow

Verify (original)


$5(0) - 20(1) < 0$

$-20 < 0$

\checkmark



dotted line



$y = mx + b$

Ex.) Write an inequality to represent the graph:

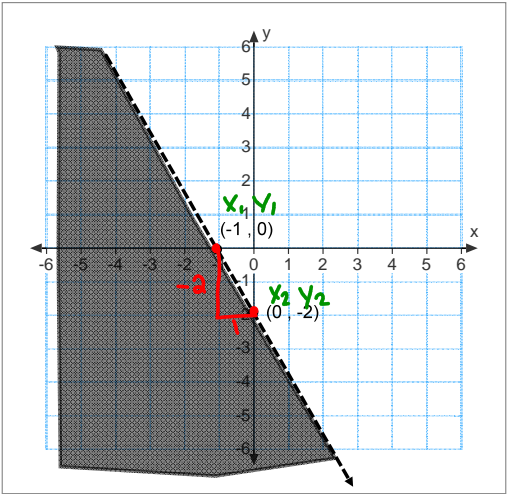
$b = -2$

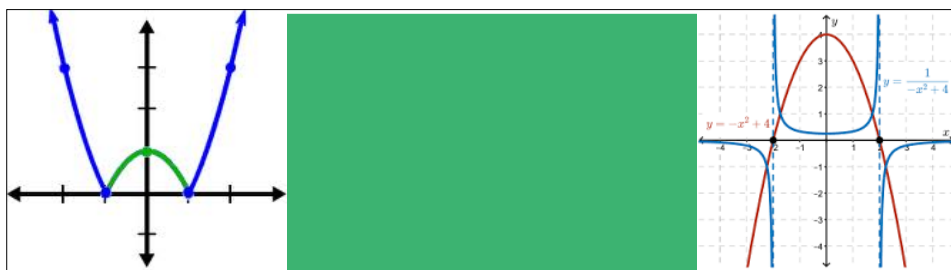
$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-2 - 0}{0 - -1}$

$= \frac{-2}{1}$

$y = mx + b$

$y < -2x - 2$



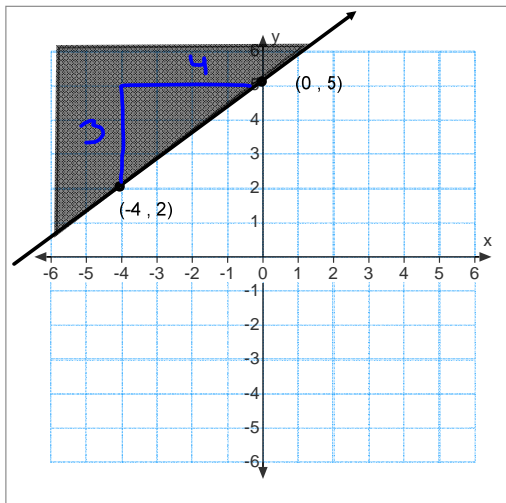


Ex.) Write an inequality to represent the graph:

$$m = \frac{3}{4}$$

$$b = 5$$

$$y \geq \frac{3}{4}x + 5$$



Ex.) You are constructing a mosaic made of tile and stone. Tile costs \$2.50/ft². Stone costs \$6.00/kg. Your budget may not exceed \$150.00. Use technology to find all possible solutions.

t = amount of tile (ft²)

s = amount of stone (kg)

$$2.50t + 6.00s \leq 150$$

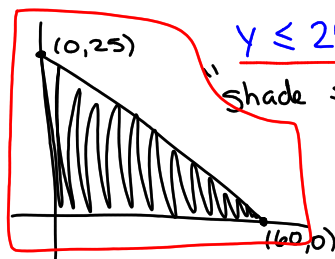
$$2.50x + 6.00y \leq 150$$

$$-2.50x \quad -2.50x$$

$$\frac{6.00y}{6} \leq \frac{150 - 2.50x}{6}$$

$$y \leq 25 - \frac{5}{12}x$$

"shade \leq graph"



Pg. 472
#1-5.